Through logic and deduction, the clues can be distributed as shown and the paths formed as indicated below. Darkening the interiors (as suggested by the introduction and the example) and re-overlaying the results gives the image shown below, letters spelling PEON left to right.


